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SARDAR PATEL UNIVERSITY
M.Sc. (IV Semester) Examination
2012

Friday, 30th November

2:30 p.m. to 5:30 p.m.

STATISTICS COURSE No. PS04CSTA01
(Computer Oriented Statistical Methods)

Note: Figures to the right indicate full marks of the questions. (Total Marks: 70)

I Attempt all, write correct answers 08

- (i) The only natural random number generation method is
- a) congruential method b) inverse method
- c) none of these d) Pi based method
- (ii) Canonical correlation analysis helps in
- a) increasing the dimension of data b) reducing the dimension of data
- c) finding the minimum possible correlation among linear combinations
- d) finding the maximum possible correlation among linear combinations
- (iii) If the random numbers are generated through multiplicative congruential method with seed 3, multiplier 11 and modulus 100 then cycle repeats after each ___ numbers.
- a) 9 b) none of these
- c) 10 d) 11
- (iv) Which of the following decomposition is used in generation of multivariate normal random numbers
- a) Jordan decomposition b) Lebesgue decomposition
- c) Cholesky decomposition d) singular value decomposition
- (v) The inverse function of the Triangular distribution function $\frac{2}{a}(x - \frac{x^2}{2a})$ as per inverse method is
- a) $a(1-U)$ b) $a(1-\sqrt{U})$
- c) $a(1-\sqrt{2-U})$ d) $2(a-\sqrt{U})$
- (vi) The logit value is zero when the probability of event is
- a) 1 b) .5
- c) 0 d) None of these
- (vii) The Monte Carlo integration value of $\int_2^5 f(x)$
- a) 3 b) $E(f(x))$
- c) 5 d) 3 times $E(f(x))$

(viii) In variance reduction technique using control variates the data X is modified using another data Y through

- a) $-\text{Cov}(X, Y)$
- b) $-\text{Cov}(X, Y)/V(Y)$
- c) None of these
- d) $\text{Cov}(X, Y)/V(X)$

2 Attempt ANY 7, each carries 2 marks

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- (a) Describe mixed congruential method of generating random numbers with an illustration.
- (b) Prove that, If U is uniform on (0, 1), and F(x) be a d.f. with inverse d.f. $F^{-1}(\cdot)$, then $F^{-1}(U)$ has d.f. F(x).
- (c) Distinguish between parametric and non-parametric bootstrapping.
- (d) Show that the total variance of the variables equals to the total variance of the Principle Components.
- (e) Define Cox- hazard ratio of a pair of persons in the sample and show that it is not necessary to know the baseline hazard.
- (f) Write down method of generating symmetric random walk random deviates.
- (g) Explain how logistic regression approach brings out the relation between binary variable and explanatory variables.
- (h) Explain one of the variance reduction techniques.
- (i) Define the terms in the context of multivariate techniques
(i) biplot (ii) communality
- (j) Describe the method of obtaining canonical variable pairs given two sets of variables and the correlation matrix.

- 3 (a) Describe steps of Monte Carlo simulation. Discuss about the advantages and limitations of simulation. 6
- (b) Using random numbers to simulate a sample, find the probability that a packet of 8 products does not contain any defective product, when the production line produces 10 percent defective products. Compare your answer with expected probability. 6

OR

- (b) Observations showed the following patterns in respect of inter-arrival durations and service durations in a single channel queuing system.

Inter-arrival time		Service time	
Minutes	Probability	Minute	Probability
2	.15	1	.10
4	.28	3	.20
6	.40	5	.47
8	.17	7	.23

Simulate the queue behavior for a period of 90 minutes and estimate the probability of the server being idle and the mean time spent by a customer waiting for the service.

- 4 (a) Describe the main objective of canonical correlation. Show that the squared canonical correlations are the roots of the equation and that the canonical correlation vectors for variables satisfy
- $$[\Sigma_{12}\Sigma_{22}^{-1}\Sigma_{21} - \lambda\Sigma_{11}] = 0$$
- $$\Sigma_{12}\Sigma_{22}^{-1}\Sigma_{21}\alpha_i = \lambda\Sigma_{11}\alpha_i$$

- (b) Discuss the assumptions and the objective of discriminant analysis. Obtain a discriminant rule to assign an individual to one of the two multivariate normal populations such that expected cost of misclassification is minimized. Give two applications of discriminant analysis.

OR

- (b) Let $X' = [X_1, \dots, X_p]$ have covariance matrix Σ , with eigen values-eigen vector pairs $(\lambda_1, e_1), (\lambda_2, e_2), \dots, (\lambda_p, e_p)$, where $\lambda_1 \geq \lambda_2 \geq \dots \geq \lambda_p \geq 0$. Then show that the r^{th} principal component is given by $Y_r = e_r'X$, ($r=1, \dots, p$) with $\text{var}(Y_i) = \lambda_i$ and $\text{Cov}(Y_i, Y_j) = 0$ for $i \neq j = 1, 2, \dots, p$.
- 5 (a) Explain rejection method of generating random numbers, and illustrate.
- (b) Describe an algorithm for generating random deviates having (i) Weibull distribution (ii) t- distribution.

OR

- (b) Write algorithm for generating 'n' binomial $B(10, .5)$ deviates. Using your algorithm carry out generating such 5 binomial deviates.
- 6 (a) Explain what is clustering in a multivariate data set. Give an algorithm used for clustering.
- (b) Explain method of generating multivariate normal deviates. Generate four bivariate normal numbers having mean $[2, -1]'$ and covariance matrix $\begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$.

OR

- (b) Give the bootstrap algorithm for approximating the standard error of an estimator.
