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SARDAR PATEL UNIVERSITY

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M. Sc. (Physics) 4th Semester ExaminationWednesday, 6th April, 2016

Time: 02:30 pm to 05:30 pm

Subject: PS04CPHY02 [Theoretical Solid State Physics]

Total Marks: 70

Note: (1) Figures to the right indicate marks.

(2) Symbols have their traditional meaning.

Q:1 Attempt all of the following Multiple choice type questions. [01 mark each] [08]

- (1) When one includes relaxation time for scattering, frequency dependent dielectric function is given by

(a) $\left(1 - \frac{\omega_p^2}{\omega^2}\right) \frac{1}{\left(\omega + i/\tau\right)}$

(c) $\left(1 - \frac{\omega_p^2}{\omega^2}\right) \frac{1}{\left(\omega + i/\tau\right)}$

(b) $\left(\frac{\omega_p^2}{\omega}\right) \frac{1}{\left(\omega + i/\tau\right)}$

(d) $\left(1 - \frac{\omega_p}{\omega}\right) \frac{1}{\left(\omega + i/\tau\right)}$

- (2) Radius of the Fermi sphere in k-space is given by

(a) $\left(3\pi^2 n/a^3\right)^{1/2}$

(c) $\left(3\pi^2 n/a^2\right)^{1/2}$

(b) $\left(3\pi^2 n/a^2\right)^{1/3}$

(d) $\left(3\pi^2 n/a^3\right)^{1/3}$

- (3) In OPW method the electron wave function outside a ion core is assumed to be a

(a) tightly bound

(c) orthogonalized plane wave

(b) plane wave

(d) highly oscillating wave

- (4) Under the free electron approximation the E versus k curve is

(a) constant

(c) plane wave

(b) parabolic

(d) highly oscillating

- (5) For a spherical Fermi surface for a free electron case, the velocity of an electron is

(a) $v = \hbar^2 k^2 / m_0$

(c) $v = (\hbar k / m_0)^{1/2}$

(b) $v = (\hbar k / m_0)^2$

(d) $v = \hbar k / m_0$

- (6) The classical Debye-Huckel screening length is proportional to...

(a) $\left(\frac{N_0 e^2}{T}\right)^2$

(c) $\left(\frac{N_0 e^2}{T}\right)^1$

(b) $\left(\frac{N_0 e^2}{T}\right)^{1/2}$

(d) $\left(\frac{N_0 e^2}{T}\right)^{-1/2}$

(7) The transition temperature varies with average isotopic mass as

- (a) $T_c \propto M^{-1/2}$ (c) $T_c \propto M^{-1/3}$
 (b) $T_c \propto M^{-2}$ (d) $T_c \propto M^{1/2}$

(8) The London penetration depth _____ with temperature.

- (a) decreases (c) increases
 (b) remains constant (d) levels off

Q:2 Answer any 7 of the following 9 questions briefly. [02 marks each] [14]

- 1 What is Umklapp process?
- 2 Draw graphs of effective mass, energy, first order and second order derivative of energy as a function of wave vector k.
- 3 Explain how Brillouin zones are drawn with the help of suitable diagrams.
- 4 With the help of a suitable diagram show how solids are classified into conductors, semi-conductors and insulators.
- 5 What is dHvA effect?
- 6 List the methods used to experimentally find the Fermi surface.
- 7 Differentiate between type I and type II superconductors.
- 8 Explain energy gap at the Fermi level in the superconducting state.
- 9 What are Cooper pairs?

Q:3 (a) State and prove Bloch's theorem. [6]

(b) Write a detailed note on screened Coulomb potential. [6]

OR

(b) Formulate the Kronig-Penney model and establish the relation [6]

$$P \frac{\sin(\alpha a)}{\alpha a} + \cos(\alpha a) = \cos(ka)$$

Q:4 (a) Explain the empty lattice method of band structure calculation. What are the drawbacks of this method? [6]

(b) Explain the plane wave method of band structure calculation. [6]

OR

(b) Explain the tight binding method of energy band calculation. [6]

Q:5 (a) Write a note on effect of magnetic field on Fermi surface. [6]

(b) Write a note on quantization of electron orbits and show that the radius of [6]

$$\text{the } n\text{th orbit is } r_n = \left[\frac{2\hbar}{m_o \omega_c} \left(n + \frac{1}{2} \right) \right]^{1/2}$$

OR

(b) Derive Hamiltonian for interacting electron gas in terms of density [6]

- Q:6 (a) Explain the Meissner effect and prove that superconductivity is [6]
diamagnetism of a different kind.
- (b) Discuss various thermodynamic properties of a superconductor. Prove that [6]
normal to superconducting phase transition is a second order phase
transition.

OR

- (b) Write notes on (i) BCS ground state and (ii) Fullerenes. [6]

$$\chi' = \chi'' = \chi$$