SEAT No.

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## SARDAR PATEL UNIVERSITY

M. Sc. (Physics) 1<sup>st</sup> Semester Examination Monday, 22<sup>nd</sup> October, 2018 Time: 10:00 am to 01:00 pm

Subject: PS01CPHY21 [Mathematical Physics]

Total Marks: 70

Note: (1) Figures to the right indicate marks.

(2) Symbols have their traditional meaning.

## Q:1 Attempt all of the following Multiple choice type questions. [01 mark each ] [08]

(1)  $\langle \phi | \psi \rangle^* =$ 

(a)  $\langle \psi | \phi \rangle$ 

(c)  $\langle \psi^* | \phi^* \rangle$ 

(b)  $\langle \psi | \phi \rangle$ 

(d)

(2)  $\langle c | d \rangle = \alpha \langle c | a \rangle + \beta \langle c | b \rangle$ 

(a) is a linear function of a and b.

(c) is not a linear function  $\alpha$  and  $\beta$ .

(b) is a linear function of  $\alpha$  and  $\beta$ .

(d) is called a functional.

(3) In the Laurent series expansion of  $\frac{e^z}{z^4}$ , the coefficient  $b_1$  i.e. the residue is

(a) 1/4!

(c) 1/2!

(b)  $2\pi i$ 

(d) 1/3!

(4) If c is a circle  $|z-z_0| = r$ ,  $\int_{c} \frac{dz}{(z-z_0)^2}$  will be equal to

(a)  $2\pi i$ 

(c)  $-2\pi i$ 

(b) = 0

(d) ∞

(5) The Fourier transform of an odd function is equivalent to its

(a) sine transform

(c) Henkel transform

(b) Melin transform

(d) cosine transform

(6) The Laplace transform of  $t^3$  is given by

(a) s-3

(c)  $6/s^4$ 

(b)  $1/s^3$ 

(d)  $6/s^3$ 

(7) The covariant derivative of a metric tensor is equal to

(a) Dirac delta function

(c) one

(b) does not exist

(d) zero

(8) The number of generators of S U(x) is

(a)  $2^{n+1}$ 

(c)  $n^2 + 1$ 

(b)  $2^n$ 

(d)  $n^2 - 1$ 

- Q:2 Answer any 7 of the following 9 questions briefly. [02 marks each] [14]
  - 1 Explain Cauchy-Schwarz inequality.
  - Show that a vector  $|a\rangle$  multiplied by number 0 gives  $|0\rangle$ .
  - 3 Explain essential singularity using a suitable example.
  - Show that  $\oint_{C} \frac{dz}{(z-z_0)} = 2\pi i$ .
  - 5 Define simple pole and simply connected region.
  - 6 Describe the RLC analogy.
  - Write the Parseval's relation and give its significance.
  - 8 What is quotient rule.
  - 9 Explain homomorphism and isomorphism.
- Q:3 (a) Define linear vector space. Explain scalar product.

[6]

[6]

[6]

- (b) (i) Norm and scalar product.
  - (ii) Explain self adjointness.

OR

(b) Two vectors in a three dimensional vector space are defined by:

$$|A\rangle = \begin{pmatrix} 2 \\ -7i \\ 1 \end{pmatrix}, |B\rangle = \begin{pmatrix} 1+3i \\ 4 \\ 8 \end{pmatrix}.$$

Given a=6+5i, Compute  $a|A\rangle$ ,  $a|B\rangle$ ,  $\langle A|B\rangle$  and  $\langle B|A\rangle$ .

- Q:4 (a) State and prove Cauchy-Riemann conditions. Evaluate  $\oint_c \frac{\sin(3z)}{z + \frac{\pi}{2}} dz$  if c is a circle |z| = 5.
  - (b) Write a note on Mapping.

[6]

OR

(b) If f(z) is single valued and analytic throughout a simply connected region [6] R, then the line integral of f(z) around any closed path c which lies entirely inside R is zero i.e.  $\oint_c f(z) dz = 0$ . Evaluate  $\oint_c \frac{z^2 + 4z - 2}{z - 4} dz$  over a contour path enclosing the pole  $z_0 = 4$ .

- Q:5 (a) Obtain the solution of a damped oscillator using Laplace transform, given by equation  $mx''(t) + bx'(t) + kx(t) = 0 \text{ with initial conditions } x(0) = x_0, x'(0) = 0.$ 
  - (b) Obtain the Fourier transform of a finite wave train. Using the result derive [6] the energy-time uncertainty relation.

## OR

- (b) Write notes on (i) convolution theorem (ii) Fourier transform of [6] derivatives.
- Q:6 (a) Write notes on (i) metric tensor (ii) geodetic equation. [6]
  - (b) Write notes on (i) Christoffel symbol (ii) covariant derivative. [6]

## OR

(b) With proper illustrations, write a detailed note on the group concept in [6] various branches of physics.

