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**SARDAR PATEL UNIVERSITY**  
**M. Sc. Physics I<sup>st</sup> Semester Examination**  
**Monday, Date: 11-04-2016 Time: 10.30 AM to 01.30 PM**  
**CBCS Course No.: PS01CPHY03**  
**Subject: Atomic Molecular & Laser Physics**

Note: Symbols have their usual meaning.

Total Marks: 70

**Q.1 Write answers of all eight questions in a table form by showing your choice against the question number. (8)**

- (1) In the case of H-atom "centrifugal barrier potential" varies as \_\_\_\_\_.  
(a)  $\frac{1}{r}$  (b)  $\frac{1}{r^2}$  (c)  $\frac{1}{r^3}$  (d)  $r^2$
- (2) For three level laser system, \_\_\_\_\_ gives necessary mathematical condition for population inversion between level 1 and 2.  
(a)  $T_{32} = T_{21}$  (b)  $T_{32} > T_{21}$  (c)  $T_{32} < T_{21}$  (d)  $T_{32} > T_{31}$
- (3) Most probable decay mechanism of  $2S_{1/2}$  is \_\_\_\_\_.  
(a) non-radiative transition (b) one-photon spontaneous radiation  
(c) two-photon emission (d) completely forbidden
- (4) Life time for cavity photon in a given lasing system depends on \_\_\_\_\_.  
(a) internal absorption (b) leakage through window (mirror-2)  
(c) scattering (d) all of the above
- (5) \_\_\_\_\_ gas is used to increase the efficiency of the  $CO_2$  gas laser.  
(a) He (b)  $N_2$  (c)  $O_2$  (d)  $NH_3$
- (6) The energy difference between various vibrational levels corresponds to the \_\_\_\_\_ region.  
(a) infrared (b) visible (c) ultraviolet (d) far infrared
- (7) Angle between HOH in  $H_2O$  molecule is more than  $90^\circ$ , because of \_\_\_\_\_.  
(a) repulsion between electrons (b) stretching effect of rotation  
(c) hybridization effect of 2s and 2p orbitals (d) dipolar nature of  $H_2O$
- (8) Which of the following does not fall in the microwave region?  
(a) ESR (b) hyperfine structure (c) Lamb shift (d) Lyman- $\alpha$  line

**Q.2 Answer any seven questions. (14)**

- (1) "Rydberg atoms can be treated as hydrogenic atoms" – why?
- (2) Obtain the eigenvalue of *permutation* or *interchange* operator.
- (3) With usual notation, prove that for two electron system,  $S_z \chi_1(1,2) = \chi_1(1,2)$ .
- (4) Write two assumptions involved in Thomas-Fermi model for many-electron atom.
- (5) Draw a simple diagram showing a few rotational levels for the ground vibrational states in a molecule.
- (6) Why normal optical sources do not emit stimulated light?

- (7) What are cold atoms?  
 (8) Give difference between Rayleigh and Raman scattering.  
 (9) Briefly describe the basic principle of free electron laser.

Q.3 (a) For H-atom, setup Hamiltonian and derive  $\left[\frac{d^2}{d\rho^2} - \frac{l(l+1)}{\rho^2} + \frac{\lambda}{\rho} - \frac{1}{4}\right] u_{E,l}(\rho) = 0$ . (6)

Here,  $\rho = \left(-\frac{8\mu E}{\hbar^2}\right)^{-\frac{1}{2}} r$  and  $\lambda = \frac{Ze^2}{4\pi\epsilon_0\hbar} \left(-\frac{\mu}{2E}\right)^{-\frac{1}{2}}$  for bound state ( $E < 0$ ).

- (b) Write detailed note on Lamb shift experiment. (6)

OR

- (b) Write expression for Hamiltonian for two-electron system. Based on the Pauli's (6)  
 exclusion principle, discuss the symmetric and antisymmetric properties of wave  
 function.

Q.4 (a) Derive  $\frac{d^2\chi(x)}{dx^2(x)} - \frac{1}{\sqrt{x}}[\chi(x)]^{\frac{3}{2}} = 0$  using Thomas-Fermi theory for many-electron (6)  
 atoms. Write at least one limitation of the theory.

- (b) Give detailed note on LCAO method considering an example of  $H_2^+$  ion. (6)

OR

- (b) Based on Born-Oppenheimer approximation, derive an equation for total (6)  
 energy ( $E_{s,v,j}$ ) for diatomic molecule. Discuss the use of Morse potential in  
 determining  $E_{s,v,j}$ .

Q.5 (a) Derive necessary equations to show how variation of Laser power around (6)  
 threshold condition take place.

- (b) For three-level laser system, obtain the condition for population inversion, and (6)  
 derive an expression for threshold pump power. Average pump frequency of a  
 given three-level Ruby laser is  $6.25 \times 10^{14}$  Hz. Density of  $Cr^{+3}$  ions and threshold  
 pump rate ( $W_{pt}$ ) are  $1.6 \times 10^{19}$  cc and  $330 \text{ s}^{-1}$ . Calculate threshold pump power.

OR

- (b) Using an expression  $\Gamma_{12} = \frac{1}{2\epsilon_0} \frac{D_{21}^2}{\hbar^2} \int u(\omega) \left\{ \frac{\sin[(\omega_{21}-\omega)/2]t}{(\omega_{21}-\omega)/2} \right\}^2 d\omega$  for transition (6)  
 probability and assuming  $u(\omega)$  varies slowly, obtain expressions for Einstein  
 coefficients  $B_{12}$  and  $A$ .

Q.6 (a) Write detailed note on semiconductor laser. (6)

- (b) Write the basic principle of laser. Discuss the working of He-Ne laser with (6)  
 the help of suitable diagram. Why only specific dimension of He-Ne discharge  
 tube is selected?

OR

- (b) Write detailed note on  $NH_3$  maser. (6)

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