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SARDAR PATEL UNIVERSITY

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M. Sc. (Physics) 1st Semester ExaminationTuesday, 21st April, 2015

Time: 10:30 am to 01:30 pm

Subject: PS01CPHY01 [Mathematical Physics & Computer Programming]

Total Marks: 70

- Note: (1) Figures to the right indicate marks.
 (2) Symbols have their traditional meaning.

Q:1 Attempt all of the following Multiple choice type questions. [01 mark each] [08]

- (1) The number of components in a tensor of rank 2 in 3 dimensional space is
 (a) 9 (c) 27
 (b) 3 (d) 81
- (2) A technique for creating new, higher rank tensors is
 (a) Inner product (c) Cauchy-Schwartz inequality
 (b) direct product (d) quotient rule
- (3) $\oint_C \frac{z^2}{z-2}$ where C is $|z|=1$ is
 (a) 0 (c) πi
 (b) $2\pi i$ (d) $4\pi i$
- (4) For a complex variable z , $z+z^*$ is equal to
 (a) zero (c) imaginary
 (b) real (d) complex
- (5) The Laplace transform of 1 i.e. $\mathcal{L}\{1\}$ is
 (a) s^2 (c) $1/s$
 (b) 1 (d) s
- (6) Integral transform based on the kernel $e^{i\omega x}$ if known as
 (a) Laplace transform (c) Mellin transform
 (b) Henkel transform (d) Fourier transform
- (7) For a DO loop, DO I = -10,2 the number of iterations will be
 (a) 10 (c) 13
 (b) 0 (d) 12
- (8) If $i=45$ then $10*i/10$ gives
 (a) 4.5 (c) 0
 (b) 40 (d) 45

Q:2 Answer any 7 of the following 9 questions briefly. [02 marks each] [14]

- 1 Define (i) unitary operator (ii) eigen value.
- 2 Explain quotient rule.
- 3 Show that z^2 is analytic.
- 4 Define complex quantity. Show that zz^* is a real quantity.
- 5 Define Laplace transform.
- 6 Explain the term "convolution".
- 7 Explain IF-ELSEIF statement using example.
- 8 Write full form of FORTRAN. How is a FORTRAN program compiled?
- 9 Define with suitable examples constants and variables.

Q:3 (a) Define Hermitian operator and prove that its Eigen values are real [6]
quantities. Also explain projection operators.

(b) Write note on types of tensors and their algebra. [6]

OR

(b) Write notes on (i) covariant derivative (ii) geodesic equation. [6]

Q:4 (a) If $f(z)$ is a single valued and analytic throughout a simply connected region R , and if c is any closed contour interior to R and enclosing z_0 , then show [6]

$$\text{that } f(z_0) = \frac{1}{2\pi i} \oint_c \frac{f(z)}{(z - z_0)} dz.$$

(b) Define Green's function. Obtain Green's function for $\frac{d^2 y}{dx^2} + k^2 y = f(x)$ [6]
where $y(\pm\infty) = 0$.

OR

(b) Discuss in short conformal mapping. Discuss the mapping of $w=z^2$. [6]

Q:5 (a) Obtain Laplace transform for the damped oscillator. [6]

(b) Using proper integral transform, explain how a finite pulse could be [6]
resolved into sinusoidal waves.

OR

(b) With proper illustrations, write a detailed note on the group concept in [6]
various branches of physics.

Q:6 (a) Write a short note on DO loops. Write a FORTRAN90 program to compute [6]
the sum of even integers making use of DO loops.

(b) Write short notes on (i) arithmetic expressions (ii) input-output statements. [6]

OR

(b) Explain format specifications with the help of suitable examples. [6]

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