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SARDAR PATEL UNIVERSITY
M. Sc. Information Technology
 Semester – I External ATKT Examinations
PS01CINT03 – Introduction to Theoretical Computer Science
 25th April 2015

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Time: 10:30 a.m. to 01:30 p.m.

Max Marks: 70

Q1. Choose the most appropriate option for each question.

[8]

- [1] "Number of fish in Indian Ocean" set is
 [A] Finite [B] Countable finite
 [C] Uncountably finite [D] None of these
- [2] IF $A = \{5,7,8\}$ and $B = \{2,5,9,11,12\}$, then $A - B$ equals
 [A] $\{2,5,7,8,9\}$ [B] $\{7,8\}$
 [C] $\{2,5,7,8,9,11,12\}$ [D] None of these
- [3] A Lattice (L, \leq) is called a _____ if it has a greatest element denoted by 1 and a least element denoted by 0.
 [A] Grounded Lattice [B] Complete Lattice
 [C] Bounded Lattice [D] Complemented Lattice
- [4] A decline or changes that have occurred in ice-cream sales during November to February is called _____ variation.
 [A] Trend [B] Seasonal
 [C] Cyclic [D] Irregular
- [5] According to rule of product if experiment 1 has 7 outcomes and experiment 2 has 3 outcomes then there are _____ possible outcomes.
 [A] 10 [B] 11
 [C] 20 [D] 21
- [6] The size of set $\{\{a,b\}\}$ is _____.
 [A] 1 [B] 2
 [C] 3 [D] None of these
- [7] A function $f: A \rightarrow B$ is said to be _____ if for each $b \in B$, there exists at most one $a \in A$ with $f(x) = y$.
 [A] Bijective [B] Injective
 [C] Surjective [D] Objective
- [8] If there is an edge (a, b) between vertex a and b , then vertex a is said to be _____ to vertex b .
 [A] adjacent [B] non-terminal
 [C] equal [D] None of these

Q2. Answer the following questions (Any Seven):

[14]

- Define with an example: Lattice; Bounded Lattice.
- Explain rule of sum and product.
- Explain Weighted graphs and multigraphs.
- Draw a Truth table for $(P \wedge Q) \vee (P \wedge R)$.
- Explain in brief Infinite sets.
- Define with an example: Binary relation.
- What is isomorphic graph? Give an example.

- h. Define and give any one example of fuzzy set.
- i. State that the formula $(P \vee Q) \Rightarrow (\sim P)$ is a tautology or not by giving truth table.

Q3. Answer the following questions:

- a. Explain properties of binary relations with suitable example. [6]
- b. Explain Phrase Structure grammar with example. Also explain how phrase structure grammar can be used to specify language. [6]

OR

- b. Define Algorithm. Write down the LARGEST1 algorithm to find largest value from n numbers. [6]

Q-4 Answer the following questions:

- a. Fit a Straight line trend for the following series. Estimate the value for 2015. [6]

Year	2004	2005	2006	2007	2008	2009	2010
Earnings (Rs. Lakhs)	60	72	75	65	80	85	95

- b. Explain components and utilities of time series with example. [6]

OR

- b. Fit a parabola $Y = a + bX + cX^2$ using given data: [6]

Year	2011	2012	2013	2014	2015
Production('000)	5	7	4	9	10

Estimate the value for 2018.

Q-5 Answer the following questions:

- a. Explain Boolean Algebra and Boolean Lattices in detail. [6]
- b. Write a detailed note on complexity of problems. [6]

OR

- b. Prove that in a graph G with n vertices, if there is a path from vertex v_1 to vertex v_2 , then there is a path of no more than $n - 1$ edges from vertex v_1 to vertex v_2 . [6]

Q-6 Answer the following questions:

- a. Let G be a linear graph of n vertices. If the sum of the degrees for each pair of vertices in G is $n - 1$ or larger, then prove that there exists a Hamiltonian path in G. [6]
- b. Mention fuzzy relations (i) Union, (ii) Intersection and (iii) Complement by giving an example of each. [6]

OR

- b. Define fuzzy proposition and solve the following [6]

Let \tilde{P} : Jessica is efficient $T(\tilde{P}) = 0.7$

And \tilde{Q} : John is efficient $T(\tilde{Q}) = 0.55$

(i) $T(\tilde{P} \vee \tilde{Q})$ Either Jessica or John is efficient

(ii) $\tilde{P} \Rightarrow \tilde{Q}$ If Jessica is efficient then so is John.