

SARDAR PATEL UNIVERSITY

[21/A-21]

M.Sc. Integrated Biotechnology, First semester

Subject Code: PS01CIGB06

Subject Title: Biomathematics

Date:24/04/2018

Time:02:00pm to 05:00pm

Day:Tuesday

Total Marks:70

Note:Figures to the right indicate marks.

- Q-1 Choose the best appropriate alternative for the following:** [08]
- 1 If $f(x)$ represents parabola opening upward, $f(x)$ can be _____.
(a) $-2x$ (b) 5 (c) $-2x^2+9$ (d) $2x^2+9$
 - 2 Derivative of $2x^4$ is _____.
(a) $18x^3$ (b) $8x^3$ (c) $2x^3$ (d) None of these
 - 3 Partial derivative of xy with respect to x is _____.
(a) x (b) y (c) 0 (d) None of these
 - 4 Integration of $2\cos x$ is _____.
(a) $2\sin x$ (b) $-2\sin x$ (c) $(\sin x)/2$ (d) None of these
 - 5 If $f'(x_0)=0, x_0$ is called _____.
(a) Maxima (b) Minima (c) Extrema (d) None of these
 - 6 If A is a 3×3 matrix whose inverse exists, then the rank of A is _____.
(a) ≥ 3 (b) ≤ 3 (c) 3 (d) Is not defined
 - 7 Which of the following property does not hold for matrix multiplication?
(a) Commutative (b) Distributive (c) Both (d) None of these
 - 8 If $f:A \rightarrow B$ is a function, A is called _____.
(a) Domain (b) Range (c) Codomain (d) None of these

- Q-2 Attempt any seven of the following:** [14]
- 1 Find coordinates of vertex of the parabola $y = -2x^2 + 15x + 9$
 - 2 Determine slope and y-intercept for $9x - 2y + 5 = 0$.
 - 3 Evaluate: $\lim_{x \rightarrow 3} \frac{x^3 - 27}{x^2 - 9}$.
 - 4 Find $\frac{dy}{dx}$ for $y = e^{5x}$.
 - 5 Find $\frac{\partial z}{\partial x}$ if $z = x^2 + y^2$.
 - 6 Identify order and degree of the differential equation:
$$\left(\frac{d^2 y}{dx^2}\right)^4 + 9\left(\frac{dy}{dx}\right) - 7xy = 0.$$
 - 7 Evaluate $3A - 2B$ if $A = \begin{pmatrix} -2 & 2 \\ -1 & 1 \end{pmatrix}$ and $B = \begin{pmatrix} 4 & -1 \\ 1 & 4 \end{pmatrix}$.
 - 8 Define: (i) Equality of matrices (ii) Skew symmetric matrix.
 - 9 Explain Row echelon form of a matrix.

- Q-3 A Define Power function. Describe various shapes of power function for different values of n. [06]
- B (i) Find domain and range of the function $f(x) = \frac{2x-1}{x-5}$. [06]
(ii) Solve: $\log x + \log 2 = \log 5 - \log x$.
OR
- B (i) Prove that $\frac{\tan x + \sec x}{\tan x - \sec x} = \frac{1 + \operatorname{cosec} x}{1 - \operatorname{cosec} x}$. [06]
(ii) Give equation of a straight line passing through (1,5) and (2,4). [06]
- Q-4 A Evaluate: (i) $\lim_{x \rightarrow 0} \frac{5^x - 9^x}{\sin x}$ (ii) $\lim_{n \rightarrow \infty} \frac{11n^5 + 7n^3 + n^2 + 1}{15n^5 + 8n^3 + 3n^2 + 15}$. [06]
- B Find $\frac{dy}{dx}$ for (i) $y = \sin(\log x)$ (ii) $y = \frac{2x^2 + 1}{5x}$.
OR
- B Define local maxima and local minimum for a function of single variable. Find local maximum and local minimum value for $f(x) = (\log x)/x$, if they exist. [06]
- Q-5 A Find all second order partial derivatives for $z = xy$. [06]
B Find the local minimum value for the function of two variables: $f(x,y) = 2x^2 + 2y^2 + xy$. [06]
- B Evaluate (i) $\int x \sin x dx$ (ii) $\int (x^3 + 3x^2 + 8x + 11) dx$ [06]
- Q-6 A Find the inverse of the matrix $\begin{bmatrix} 2 & 1 & 3 \\ 4 & 2 & -1 \\ 2 & -1 & -1 \end{bmatrix}$ [06]
- B Find the eigenvalues and the corresponding eigenvectors of the matrix $\begin{bmatrix} 3 & 5 \\ -2 & -4 \end{bmatrix}$. [06]
- B Find the eigenvalues and the corresponding eigenvectors of the matrix $\begin{bmatrix} 5 & 2 & 2 \\ 3 & 6 & 3 \\ 6 & 6 & 9 \end{bmatrix}$. [06]