

(61-A)

SARDAR PATEL UNIVERSITY

M.Sc. (Electronics and Communication) (SEM – I) Examination 2012

Day & Date: 5/12/2012, Wednesday

Time: 10:30 am To 1:30 pm

Course Code: PS01CELC03

Course: Signals and Systems

Note:

(a) Figure to the right indicates maximum marks.

Total Marks: 70

(b) All questions are compulsory.

Q-1 Multiple Choice Questions

(08)

1. An analog electrocardiogram signal contains a frequency up to 100 Hz. What is the Nyquist rate for the signal?
 (A) 50 Hz (B) 100 Hz (C) 200 Hz (D) 300 Hz
2. If the discrete time sampled signal is given by $x(n) = 3 \cos\left(\frac{\pi n}{2}\right)$ with $F_s = 300$ Hz, what is the continuous time signal obtain using ideal interpolation?
 (A) $x(t) = 3 \cos(300\pi t)$ (B) $x(t) = 3 \cos(150\pi t)$ (C) $x(t) = 3 \cos(75\pi t)$ (D) $x(t) = 3 \cos(0.25\pi t)$
3. Which of the following statement is true?
 (i) A static system is memory less system
 (ii) A dynamic system has a finite or infinite memory.
 (A) (i) is true (B) (ii) is true (C) (i) and (ii) is both (D) Neither (i) Nor (ii)
4. If $x(n) = \left\{1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \frac{1}{64}, \frac{1}{128}\right\}$ then $x(4-n) =$ _____
 (A) $\left\{\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \frac{1}{64}, \frac{1}{128}\right\}$ (B) $x(n) = \left\{1, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \frac{1}{64}, \frac{1}{128}\right\}$ (C) $x(n) = \left\{0, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \frac{1}{64}, \frac{1}{128}\right\}$ (D) $x(n) = \left\{0, \frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{32}, \frac{1}{64}, \frac{1}{128}\right\}$
5. The z - transform of $a^n u(n) =$ _____
 (A) 1 (B) $\frac{1}{1-az^{-1}}$ (C) $\frac{z^{-1}}{1-az^{-1}}$ (D) $\frac{az^{-1}}{1-az^{-1}}$
6. The ROC of the Z transform of the discrete time sequence $x(n) = \left(\frac{1}{3}\right)^n u(n) - \left(\frac{1}{2}\right)^n u(-n-1)$ is
 (A) $\frac{1}{3} < |z| < \frac{1}{2}$ (B) $|z| > \frac{1}{2}$ (C) $|z| < \frac{1}{3}$ (D) $2 < |z| < 3$
7. The average power of the discrete time periodic signal with period N is defined as
 (A) $p_x = \frac{1}{N} \sum_{n=0}^{N-1} |x(n)|^2$ (B) $p_x = \sum_{n=0}^{N-1} |x(n)|^2$ (C) $p_x = \frac{1}{N} \sum_{n=0}^{N-1} |x(n)|$ (D) $p_x = \sum_{n=0}^{N-1} |x(n)|$
8. The N point DFT of $\delta(n)$ is
 (A) 1 (B) $\frac{j2\pi kn}{N}$ (C) $\frac{-j2\pi kn}{N}$ (D) $e^{-j2\pi kn/N}$

Q-2 Answer the following Questions. (Any Seven)

(14)

- Write the properties of Continuous time sinusoidal signal and discrete time sinusoidal signal.
- Explain symmetric and anti-symmetric signal with example.

P.T.O

3. A discrete time signal $x(n) = \{1, -1, 2, 5, 1\}$ sketch the advanced sequence and delayed sequence by 2 samples.
4. Mention and draw the ROC of the all finite duration sequences.
5. Determine the z-transform and ROC of the signal $x(n) = [3(2)^n - 4(3)^n] u(n)$.
6. Give the Dirichlet conditions.
7. Write the synthesis and analysis equations for a continuous time periodic signal and a-periodic signal.
8. Determine all the values in the 4-point twiddle factor matrix.
9. Explain the circular time shift and circular frequency shift properties of DFT.

Q-3 (A) What do you mean by Sampling? State the sampling theorem and discuss the sampling of an analog signal. (06)

(B) Determine whether the following signals are periodic or not, if periodic then find their period (06)

(i) $x(n) = 2\cos\left(\frac{n\pi}{4}\right) - \sin\left(\frac{n\pi}{6}\right) + 3\cos\left(\frac{n\pi}{8} + \frac{\pi}{3}\right)$ (ii) $x(n) = \cos\left(\frac{32\pi n}{10}\right)$ (iii) $x(n) = \cos\left(\frac{n\pi}{6}\right)\cos\left(\frac{n\pi}{9}\right)$

OR

(B) Discuss in detail classification of discrete time systems with example of each. (06)

Q-4 (A) Determine the convolution sum of the following discrete time signals using graphical method and verify it by tabular method (06)

$x(n) = \{1, 2, 0, 1, 2\}$ and $h(n) = \{1, -2, -3, 4\}$

(B) Determine the total response $y(n)$ of the system described by following input output difference equations. $y(n) - 0.75y(n-1) + 0.125y(n-2) = x(n)$ with $x(n) = u(n)$ (06)

OR

(B) Using power series expansion method, determine inverse z-transform of (06)

$X(z) = \frac{1+2z^{-1}}{1-2z^{-1}+z^{-2}}$ If (a) $x(n)$ is causal (b) $x(n)$ is anti causal

Q-5 (A) Determine the z-transform and ROC of the following (06)

(i) $x(n) = a^n (\cos \omega_0 n) u(n)$ (ii) $x(n) = na^n u(n)$ (iii) $x(n) = (1+n)u(n)$

(B) Determine the inverse z transform using partial fraction expansion and find $x(n)$ (06)

$X(z) = \frac{1}{1-1.5z^{-1}+0.5z^{-2}}$ if $x(n)$ is causal and anti causal

OR

(B) Why we need the frequency analysis of discrete time signal? Obtain the discrete time Fourier series co-efficient C_k in terms of complex exponential. (06)

Q-6 (A) Define circular convolution and perform the circular convolution for the following two sequences $x_1(n) = \{2, 1, 2, 1\}$ and $x_2(n) = \{1, 2, 3, 4\}$ (06)

(B) What is Power Density Spectrum? Derive the power density spectrum for periodic discrete time signal. (06)

OR

(B) Compute the 4 point DFT of sequence $x(n) = \{1, 2, 3, 4\}$ using direct equation method (06)

and plot magnitude and phase spectrum of the DFT.