

M.Sc. Applied Statistics Semester IV (NC)  
PS04EAST22:Econometrics  
December 29, 2020, Tuesday

Marks: 70

Times: 10:00 a.m. to 12:00 p.m.

Q1(a) Multiple Choice Questions:

- i. In context to scaling of residuals in the regression analysis,  $|t_i| > 3$  indicates, presence of \_\_\_\_\_ in data.
 

(a) Leverage point	(b) Influential point
(c) outlier	(d) Extreme point
  
- ii. In usual notation, in context ridge regression, the MSE of ridge estimator ( $MSE(\hat{\beta}_R)$ ) is defined by \_\_\_\_\_.
 

(a) $\sum_{j=1}^k \left[ \frac{\sigma^2 \lambda_j + \vartheta^2}{(\lambda_j + \vartheta)^2} \right]$	(b) $\sum_{j=1}^k \left[ \frac{\sigma^2 \lambda_j + \vartheta^2 \beta_j^2}{(\lambda_j + \vartheta)^2} \right]$
(c) $\sum_{j=1}^k \left[ \frac{\sigma^2 + \vartheta^2 \beta_j^2}{(\lambda_j + \vartheta)^2} \right]$	(d) $\sum_{j=1}^k \left[ \frac{\sigma^2 \lambda_j + \vartheta^2 \beta_j^2}{(\lambda_j + \vartheta)} \right]$
  
- iii. In context to the linear regression relation between the t and F statistic is \_\_\_\_\_.
 

(a) $t = \sqrt{F}$	(b) $t = F$
(c) $t = F^2$	(d) $F = t/N(0,1)$
  
- iv. In context to the regression analysis, if the Durbin Watson test statistic (d) is \_\_\_\_\_, then we say the presence of negative autocorrelation.
 

(a) 2	(b) 4
(c) $4 - d_L < d < 4$	(d) $0 < d < d_L$
  
- v. The Indirect Least Squares procedure of estimation is appropriate when simultaneous equations are
 

(a) Just or exact identified	(b) Over identified
(c) Not identified	(d) Under identified
  
- vi. In the simultaneous-equation models, number of structural form coefficients are less than number of reduced form coefficients then given system is
 

(a) over identified	(b) under identified
(c) exact identified	(d) recursive system
  
- vii. In context to the multicollinearity if the value of Variance Inflation Factor corresponds to j-th regressor ( $VIF_j$ ) is 10 then value of  $R_j^2$  is \_\_\_\_\_.
 

(a) 0.25	(b) 0.7
(c) 0.5	(d) 0.9
  
- viii. Multiple linear regressions with p regressors, the Cook distance statistic  $D_i$  for  $i^{th}$  point is defined as \_\_\_\_\_.
 

(a) $\frac{r_i^2 h_{ii}}{p(1-h_{ii})}$	(b) $\frac{h_{ii} r_i^2}{p}$
(c) $\frac{r_i^2 h_{ii}}{p^2(1-h_{ii})}$	(d) $\frac{r_i h_{ii}}{p^2(1-h_{ii})}$

1. Under which condition, the Principal Component Regression Analysis is applicable?
2. Define *BIC*.
3. What do you mean by Pooled data? What is an alternate name of it?
4. For the model  $y_i = \beta_0 + \beta_1 x_{i1} + \dots + \beta_k x_{ik} + \varepsilon_i$ ,  $i = 1, \dots, n$ , what is the degrees of freedom error?
5. Give the relation between the  $F$  and  $R^2$ .
6. Define endogenous variable.
7. TRUE or FALSE: In usual notation in the multiple linear regression with  $k$  variables having  $n$  observations, the distribution of Explained Sum of Square (ESS) is  $\chi_{n-k}^2$ .
8. TRUE or FALSE: The Model  $Y_i = \beta_1 + \beta_2 \left(\frac{1}{x_i}\right) + \varepsilon_i$  is known as reciprocal model.
9. TRUE or FALSE: In context to simple linear regression, the variance of future observation ( $y_0$ ) based on value of the regression variable of interest ( $x_0$ ) is 
$$\sigma^2 \left( \frac{1}{n} + \frac{(x_0 - \bar{x})^2}{s_{xx}} \right)$$
10. TRUE or FALSE: In the Classical Linear Regression Model, LS estimate and ML estimate of  $\sigma^2$  are unique.
11. TRUE or FALSE: In dummy variable regression, the Chow test is used to check presence of autocorrelation.
12. The Hausman Specification test is a test of \_\_\_\_\_.
13. In presence of the multicollinearity \_\_\_\_\_ estimator is considered to be best.
14. \_\_\_\_\_ method is used to choose appropriate value of bias constant in ridge regression.
15. \_\_\_\_\_ test of autocorrelation is also a test of model misclassification.
16. \_\_\_\_\_ point which does not affect the slope coefficient of regression line.

Q2. Short answer questions (Any Seven)

- i. Give any two definition of Econometrics.
- ii. Distinguish between  $R^2$  and Adj.  $R^2$ .
- iii. List the steps of Research Methodology of Econometrics.
- iv. Write order conditions in system of simultaneous equations.
- v. In context to the multicollinearity, define VIF and Conditional Index.
- vi. Define the heteroscedasticity. Write the name of two formal tests to detect it.
- vii. Define Durbin Watson Statistic. Give its application in Econometrics.
- viii. Define Aitken estimator. Under which condition Aitken estimator reduces to OLS estimator.
- ix. Is  $y = \exp(\beta x)$  is intrinsically linear model? Why?

- Q3 Define Classical Linear Regression Model. Further obtain OLS estimate and ML estimate of  $\underline{\beta}$  and  $\sigma^2$ . 08
- [OR]
- Q3 In usual notation, discuss constraint least squares method. 08
- Q4 Explain tests for detecting heteroscedasticity. 08
- [OR]
- Q4 Define Autocorrelation. Is an autocorrelation creating problem in estimation of parameters in CLRM? Explain in detail. 08
- Q5 Explain dummy variable regression model. 08
- [OR]
- Q5 Explain methods to detect multicollinearity. 08
- Q6 In context of Econometrics, discuss simultaneous equations in detail. 08
- [OR]
- Q6 Is OLS method suitable to estimate parameters in simultaneous equations? Why? Further discuss estimation method, when system is exact identified. 08

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