SARDAR PATEL UNIVERSITY

Programme & Subject: M.Sc (Mathematics)

Semester: IV

Syllabus with Effect from: November-2013

Paper Code: PS04EMTH31	Total Credit: 4
Title Of Paper: Algebra - II	Total Cicuit. 4

Unit	Description in detail	Weighting (%)
I	Modules, definition and examples, modules over a division ring, submodules	
	and direct sums, products and quotient modules, R-homomorphisms, first	
	isomorphism theorem, second isomorphism theorem, third isomorphism	
	theorem.	
II	Characterization of a module multiplication on an abelian group, factorization	
	and lifting of module homomorphisms, correspondence theorem, annihilator,	25%
	torsion element and torsion module, torsion free module.	
III	External direct product and external direct sum, canonical projection, internal	
	direct sum, direct summand, exact sequence, short exact sequence, split exact	/ 3%
	sequence. Free modules, cyclic modules, finitely generated free modules,	
	invariant rank property and rank of a free module.	
IV	Infinite dimensional free modules, free modules over PIDs, invariant factor	
	theorem for sub modules, finitely generated modules over PIDs. Projective	
	and injective modules, simple and semisimple modules, characterization of	25%
	finitely generated semisimple modules, left and right semisimple rings and its	
	applications to semisimple modules.	

Basic Text & Reference Books:-

- ➤ V. Sahai and V Bist, Algebra (3/e), Narosa Publishing House, New Delhi, 2008.
- ➤ P.B. Bhattacharya, SK Jain and SR Nagpaul, Basic Abstract Algebra (2/e), Cambridge University Press, South Indian Edition 2002.
- ➤ I.S. Luthar and I.B.S. Passi, Algebra Vol 3: Modules, Narosa Publishing House, New Delhi, 2004.

