(Master of Science) (Mathematics)
(M.Sc.) (Mathematics) Semester (I)

| Course Code | PS01CMTH54 | Title of the <br> Course | Advanced Linear Algebra |
| :--- | :---: | :---: | :---: |
| Total Credits <br> of the Course | 4 | Hours per <br> Week | 4 hours |


| Course <br> Objective | The aim of this course is making students to learn about abstract concepts of <br> vector spaces, linear transformations and their properties. |
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| Course Content |  | Weightage* <br> (\%) |
| :---: | :--- | :---: |
| Unit | Description | $25 \%$ |
| 1. | Vector Space <br> Elementary Basic Concepts: <br> Definitions, Examples, Subspace, <br> Homomorphism, Isomorphism, <br> Quotient space, First homomorphism theorem, <br> Internal direct sum, External direct sum, <br> Linear combination, Linear spans, <br> Linear dependence and independence, basis, Cardinality, <br> Dual space, dual basis, second dual, <br> Annihilator, dimension of the annihilator, <br> Applications to system of Linear equations. |  |
| 2. | Linear Transformation <br> Algebra of liner transformations, <br> Minimal polynomial of a linear transformation, <br> Regular and Singular linear transformations, <br> Rank of a linear transformation, <br> Characteristic roots, <br> Matrix associated with a linear transformation, <br> Isomorphism between the space of linear transformations and the space <br> of matrices, <br> Similarity of matrices, Examples and similarity of linear <br> transformations. | $25 \%$ |
| 3. | Canonical Forms <br> Triangular forms, <br> Triangular matrix associated to a linear transformation, <br> Nilpotent transformations, <br> Existence and uniqueness of invariants of a nilpotent transformation. <br> Jordan Decomposition Form, Examples | $25 \%$ |

4. Certain properties $\boldsymbol{M}_{\boldsymbol{n}}(\boldsymbol{F})$ and Quadratics

Trace, Transpose and their properties, Jacobson's lemma, Definition and properties of determinant, Quadratic forms: diagonalization of a symmetric matrix, symmetric matrix associated to a quadratic form, classification of quadratics.

| Teaching- | Interaction based Classroom teaching |
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Learning
Methodology

| Evaluation Pattern |  |  |
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| Sr. <br> No. | Details of the Evaluation | Weightage |
| 1. | Internal Written / Practical Examination (As per CBCS R.6.8.3) | $15 \%$ |
| 2. | Internal Continuous Assessment in the form of Quizzes, Assignments, <br> and Attendance (As per CBCS R.6.8.3) | $15 \%$ |
| 3. | University Examination | $70 \%$ |

Course Outcomes: After completion of this course, student will be able to

| 1 | understand the properties of vector spaces and related illustrations |
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| 2 | analyze the properties exhibited by linear transformation and their relationships with <br> matrices |
| 3 | apply results of vector spaces and linear transformations to draw valid conclusions. |
| 4 | evaluate various types of Canonical forms of linear transformation and matrix theory <br> associated with Vector spaces |
| 5 | They would be able to apply the results for Linear Algebra in several courses of higher <br> semesters |


| Suggested References: |  |
| :--- | :--- |
| Sr. No. | References |
| 1. | Herstein I. N., Topics in Algebra, Wiley Eastern Ltd., New Delhi, 1975. |
| 2. | Kwak J. H., Hong S., Linear Algebra, (Second Edition), Birkhauser, 2004. |
| 3. | Simmons G. F., Introduction to Topology and Modern Analysis, McGraw-Hill Co., <br> Tokyo, 1963. |
| 4. | Helson H., Linear Algebra, (Second Edition), Hindustan Book Agency, TRIM-4, <br> 1994. |
| 5. | Ramachandra Rao A. and Bhimasankaram P., Linear Algebra (Second Edition), <br> Hindustan Book Agency, TRIM-19, 2000. |

On-line resources to be used if available as reference material

